

SFIT4 – description of the forward model parameter

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General

- ▶ The main control file is **sfit4.ctl** which resides in the directory `sfit4` is started in.
- ▶ The general format is **key1.key2.key3...**



General

- ▶ The main control file is **sfit4.cti** which resides in the directory sfit4 is started in.

```
# General
```

```
file.in.stalayers      = station.layers
file.in.refprofile    = reference.prf
file.in.spectrum      = spectrum
file.in.isotope       = isotope.input
file.in.solarlines    = solar.dat
file.in.linelist      = 00778.501722-01008.558278.hbin
```

```
file.out.ak_matrix= ak.out
file.out.k_matrix= k.out
file.out.g_matrix= g.out
file.out.kb_matrix= kb.out
file.out.sa_matrix= sa.out
file.out.retprofiles= rprfs.table
file.out.aprprofiles= aprfs.table
file.out.summary= summary
file.out.seinv_vector      = seinv.vector
file.out.pbpfile          = pbpfile
file.out.retprofiles      = rprfs.table
file.out.aprprofiles      = aprfs.table
```

```
# Definition for retrieval gases
```

```
gas.layers              =                41
gas.profile.list        = 03 H2O 03668 03686
gas.column.list         = C02 C2H4
gas.profile.03.correlation      =                F
gas.profile.03.logstate        =                F
```



General

- ▶ The main control file is **sfit4.ctl** which resides in the directory `sfit4` is started in.
- ▶ The general format is **key1.key2.key3...**
- ▶ This deals with some of the entries in the sections **fw** and **rt**
- ▶ **fw** defines how the forward models behaves, it includes parameters for the atmosphere, and the instrument.
- ▶ **rt** defines properties of the retrieval
- ▶ some of the parameters affecting the forward model and the retrieval are found in the section **band** and **sp**, e.g.:
 - `band.zshift.apriori` an band specific offset
 - `band.wave_factor` a scaling applied to the spectrum, multiplied to the shift.
 - `band.opd`, `band.fov` properties of the instrument
 - `sp.snr` noise (deweighting) defined on some region of the spectrum



Apodisation and Phase error



Apodisation and Phase Function

In FT spectrometry an interferogram is Fourier transformed to get a spectrum

$$S(\nu) = \int_0^{\infty} I(\Delta x) \cos(2\pi\nu x) dx \quad (1)$$

Caveats:

- ▶ Interferogram finite
- ▶ Interferogram may not be strictly symmetrical
- ▶ Beam in interferometer not strictly parallel

Hence: Equation 1 has to be modified for real world spectra

- ▶ Apodisation and phase functions define the instrumental lineshape (ILS)
- ▶ inherent feature of the instrument
- ▶ the ILS affects the spectrum and has to be accounted for
- ▶ ILS effects can mask or emulate true atmospheric features



Apodisation and Phase Function

In FT spectrometry an interferogram is Fourier transformed to get a spectrum

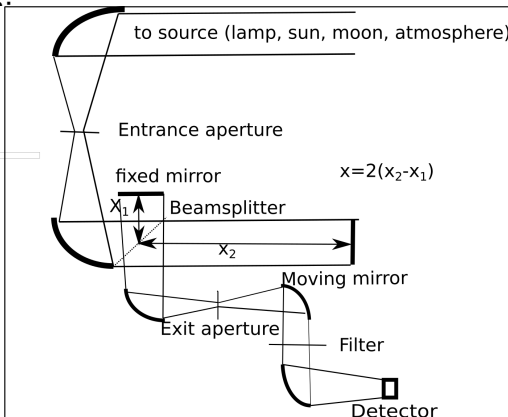
$$S(\nu) = \int_0^{\infty} I(\Delta x) \cos(2\pi\nu x) dx \quad (1)$$

Caveats:

- ▶ Int
- ▶ Int
- ▶ Be

Hence:

- ▶ Ap
- ▶ lin
- ▶ int
- ▶ the
- ▶ IL



al

world spectra

instrumental

accounted for

spheric features



Apodisation and Phase Function

How to account for the ILS in `sfit4`?

There are two 2 sources of apodisation

1. Apodisation applied while making the spectra: dealt with in `band.GAS.apodization_code`
2. Apodisation and phase error due to misalignment of the instrument

Here we are only concerned with point 2

`fw.apod_fcn` `fw.apod_function = T`

`fw.apod_function.type = 0,1,2,3,4`

`fw.apod_function.order = 1,2,3,...`

`fw.phase_fcn` `fw.phase_function = T`

`fw.phase_function.type = 0,1,2,4`

`fw.phase_function.order = 1,2,3,... (no constant!!!)`

- `rt.phase`
- ▶ set as a priori value in `rt.phase.apriori`
 - ▶ determines the constant phase offset
 - ▶ the function determined in `fw.phase_fcn` is added to it



Apodisation and Phase Function

How to account for the ILS in `sfit4`?

The structure of the files `file.in.modulation_fcn` and `file.in.phase_fcn` is:

```
jeap  
eapf(1) eapf(2) ... eapf(jeap)  
[eapx(1) eapx(2) ... eapx(jeap)]
```

`eapx` is read only when `ieap=1`.

- ▶ `jeap` simply specifies the length of the following vectors.
`eapf` is the vector of apodization parameters, whose meaning depends on `ieap`:



Apodisation and Phase Function

How to account for the ILS in *sfit4*?

ieap=1: *eapf* contains the values of the apodization function *eapdz*; in this case *eapx* contains the values of path difference at which the function is specified.

ieap=2: *eapf* contains the coefficients of a polynomial, defined by

$$eapdz = 1 + (eapf(1) - 1) * (x/xmax) + (eapf(2) - 1) * (x/xmax)^2 + \dots$$

where *x* is the path difference

ieap=3: *eapf* contains the coefficients of a Fourier series

$$\begin{aligned} eapdz = & 1 + (1 - eapf(2)) * \sin(2 * pi * eapf(1) * x/xmax) + \\ & (1 - eapf(3)) * \cos(2 * pi * eapf(1) * x/xmax) + \\ & (1 - eapf(4)) * \sin(4 * pi * eapf(1) * x/xmax) + \\ & (1 - eapf(5)) * \cos(4 * pi * eapf(1) * x/xmax) + \dots \end{aligned}$$



Apodisation and Phase Function

How to account for the ILS in sfit4?

ieap=1: eapf contains the values of the apodization function eapdz; in this case eapx contains the values of path difference at which the function is specified.

ieap=2: eapf contains the coefficients of a polynomial, defined by

$$eapdz = 1 + (eapf(1) - 1) * (x / xmax) + (eapf(2) - 1) * (x / xmax)^2 + \dots$$

NOTE: a 1 means, the the respective coefficient is ZERO

→ The parameter is the value, the ILS should have at MAX_OPD

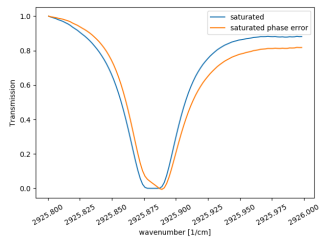
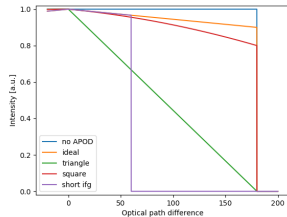
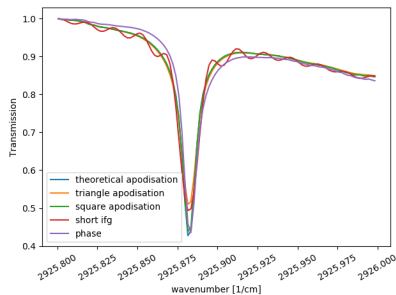
$$\begin{aligned} & (1 - eapf(3)) * \cos(2 * pi * eapf(1) * x / xmax) + \\ & (1 - eapf(4)) * \sin(4 * pi * eapf(1) * x / xmax) + \\ & (1 - eapf(5)) * \cos(4 * pi * eapf(1) * x / xmax) + \dots \end{aligned}$$



Apodisation and Phase Function

The effect of the ILS is to distort the measured spectrum: A line can be

- ▶ made broader
- ▶ made less deep
- ▶ made asymmetric
- ▶ leak to other spectral bins



Emission



Calculation of emission spectra

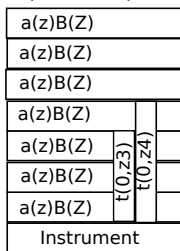
Atmospheric model

Radiance calculated by

$$I = B(\infty) \exp(-\tau(0, \infty)) + \int_0^{\infty} \underbrace{\alpha(z') B(z')}_{\text{Emission of layer } z} \exp(-\tau(0, z')) dz'$$

$$\tau(0, z) = \int_0^z \alpha(z') dz' \quad \alpha(z) = \sum_{l=1}^N x_{a,l}(z) \alpha_l(z)$$

top of atmosphere



modeled spectrum

$B(z)$ Planck function

Emission by Kirchhoff's law

$$e(\nu) = \alpha(\nu, P, T) B(\nu, T)$$

Transmission $\in [0, 1]$

$$T(0, z) = \exp(-\tau(0, z))$$



Calculation of emission spectra

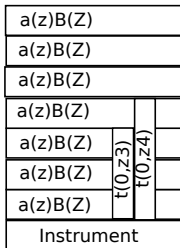
Atmospheric model

Radiance calculated by

$$I = B(\infty) \exp(-\tau(0, \infty)) + \int_0^{\infty} \underbrace{\alpha(z') B(z')}_{\text{Emission of layer } z} \exp(-\tau(0, z')) dz'$$

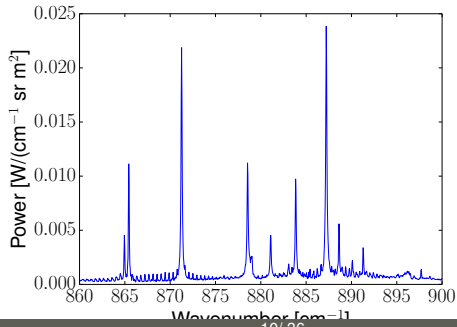
$$\tau(0, z) = \int_0^z \alpha(z') dz' \quad \alpha(z) = \sum_{l=1}^N x_{a,l}(z) \alpha_l(z)$$

top of atmosphere



modeled spectrum

Mathias Palm



Calculation of emission spectra

The calculation of the full radiative transfer is switched on by
`fw.emission = T`

The unit of the spectra is $\frac{W}{m^2 \text{srcm}^{-1}}$. The other parameters are
`fw.emission.T_infinity` the temperature of the radiation source
outside the atmosphere. This can be

`outer space`: The temperature is currently (and for
another while) 2.7K.

`Sun`: The effective temperature of the sun
is 6700K. The result is the same as
for the transmission spectra, but the
unit is $\frac{W}{m^2 \text{srcm}^{-1}}$.

`Moon` The temperature of the moon is
370.0K. Above about 3000 cm^{-1}
reflection of solar light is larger than
the blackbody emission



Cacluation of emission spectra

`fw.emission.object` used to include reflection of solar light

- `.e.` no reflection calculated

- `.m.` reflection of solar light on the moon calculated

`fw.emission.normalized` The spectra are normalized to 1. This can be used to correct spectra recorded with the moon as the light source for atmospheric emission.

this option is very seldom used, only if one has lunar measurements in transmission.



Line shape options



Line shape options

fw.lshapemodel this option offers the choice to enforce a certain lineshape model to be used.

- = 0 default and historical value. The line shape model is chosen according the spectral values available.
- = 1 enforce use of Voigt model, regardless of extra line parameters
- = 2 use Galatry if BETA_T is given, if not Voigt
- = 3 LM calculation using an adapted Voigt profile
- = 4 pCqSDHC line shape

fw.lineshapemodel.sdv use the SDV approximation in the pCqSDHC model

fw.linemixing switch on line mixing calculation (currently only 1st order)

fw.linemixing.gas currently not used



Line shape modeling

Assumptions required to arrive at the Voigt function and LBL radiative transfer

1. Binary impact theorem
-> Only two molecules interact at one time
2. Sudden impact theorem
-> The molecules are considered to be hard spheres
3. Translational and collisional effects are independent
-> Gauss and Lorentz line shape, respectively
-> Combination is Voigt line shape

$$L_V = L_G * L_L \quad (2)$$

4. Pressure broadening not a function of speed of active molecule -> Lorentz function
5. Transitions do not interact with each other
-> line-by-line calculation



Assumption: Translational and collisional effects
are independent



Dicke narrowing

Assumption: The molecules are moving at a constant speed on a straight line

Correct: Collisions may change the velocity of the molecule during the lifetime of the state

-> Collisions lead to a **Lorentz shape** of the transition (Dicke, 1953)

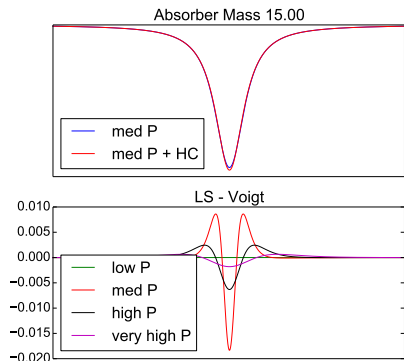
-> More frequent collisions lead to a **narrower** Doppler broadening.

Hard collision model	Soft collision model
Velocity after a collision is completely unrelated to the speed and direction before the collision	Each collision changes the velocity of the molecule only a bit, depending on the ratio (active molecule)/(perturbing molecule)
Rautian and Sobel`man (1967)	Galatry (1961)



Dicke narrowing

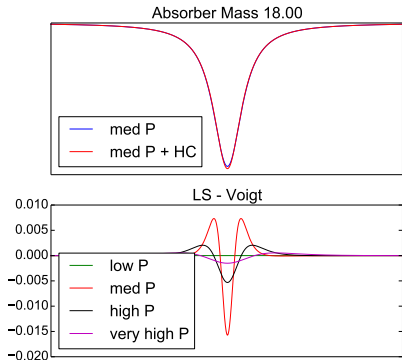
Dependency of Dicke narrowing on pressure



- ▶ Dicke narrowing modeled using hard collision model
- ▶ Effect is only present at a certain density
- ▶ At higher pressure Dicke narrowing becomes less important
- ▶ Effect most prominent if the active molecule is relatively light

Dicke narrowing

Dependency of Dicke narrowing on pressure



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- ▶ Effect is only present at a certain density
- ▶ At higher pressure Dicke narrowing becomes less important
- ▶ Effect most prominent if the active molecule is relatively light

Dicke narrowing

Due to lack of parameters for the hard collision model, Dicke narrowing is modelled only using the GALATRY lineshape model (fw.lshapemodel = 3) and for HCL and HF.

In sfit4.ctf:

```
fw.lshapemodel = 2
```

The spectroscopic input parameters are chosen in hbin.input

```
hitran.files = 99
```

...

```
014_HF/14_hit12.par
```

```
015_HCL/15_hit12.par
```

...

```
aux = gal
```

```
aux.gal.nr = 2
```

```
aux.gal.files =
```

```
014_HF/14_hit12_Galatry.txt
```

```
015_HCL/15_hit12_Galatry.txt
```

...



Dicke narrowing

Due to lack of parameters for the hard collision model, Dicke narrowing is modelled only using the GALATRY lineshape model (fw.lshapemodel = 3) and for HCL and HF.

In sfit4.ctl:

fw.lshapemodel = 2

The spectroscopic input parameters are chosen in hbin input hitran.f

...

014_H

015_H

...

aux = gal

aux.gal.nr = 2

aux.gal.files =

014_HF/14_hit12_Galatry.txt

015_HCL/15_hit12_Galatry.txt

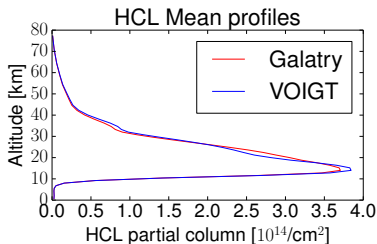
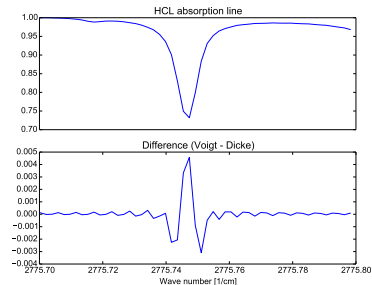
...

```
READING SOLAR LINE LIST FILE...
CALCULATION OF ASTRONOMICAL QUANTITIES ...
BAND, # SOLAR LINES FOUND      : 1    269
BAND, # SOLAR LINES FOUND      : 2    202
BAND, # SOLAR LINES FOUND      : 3    179
...
READING ATMOSPHERIC LINE LIST FILE...
HITRAN FILE : 02723.671422-02930.058578.hbin
GALATRY FLAG & LINES WITH GALATRY PARAMETERS FOUND : T    6
FCIA FLAG & FCIA LINES FOUND      : F    0
SCIA FLAG & SCIA LINES FOUND      : F    0
SDV FLAG & LINES WITH SDV PARAMETERS FOUND      : F    0
LINEMIXING FLAG & LINES WITH LINEMIXING PARAMETERS FOUND : F    0
COMPUTING CROSS-SECTIONS...
```

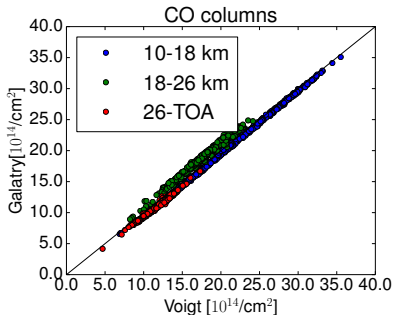


Dicke narrowing

Example: HCL



- ▶ Theoretically calculated lines with and without Dicke narrowing for the same atmospheric conditions.
- ▶ Total column does not differ, but profile



Speed dependence of pressure broadening

Assumptions: Pressure broadening not depending on speed of the molecules.

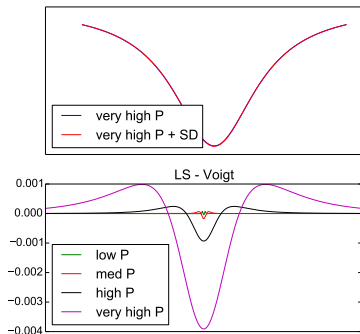
More correct: Pressure broadening depends on speed of the active molecule:

- ▶ Relative speed between active and perturbing molecules is not Maxwell Boltzmann distributed but skewed to higher velocities
- ▶ The mean of the relative speed is not given by the thermal mean of the perturber speed anymore.
- ▶ The line shape can be described by a weighted sum over Lorentz functions for different speed classes.



Speed dependence of pressure broadening

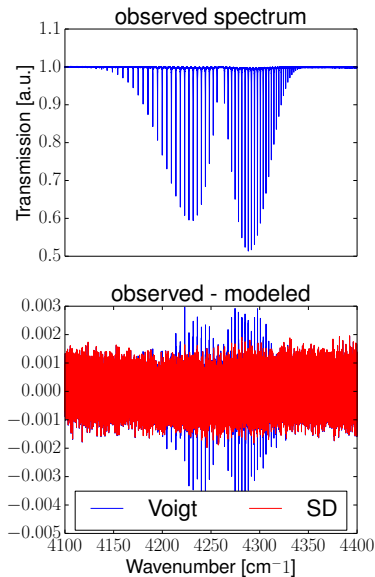
Dependency of effect on pressure



- ▶ independent on mass of molecule
- ▶ effect increases with pressure
- ▶ effect most important for gas with high abundance in troposphere



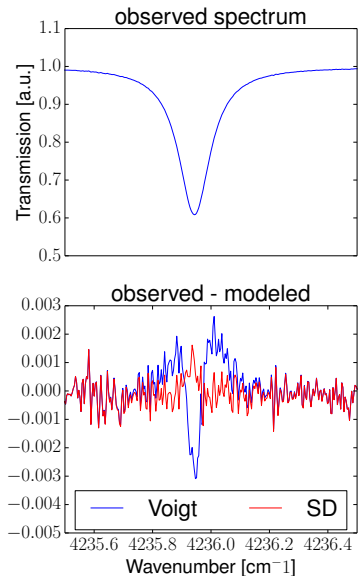
Speed dependence of pressure broadening



- ▶ Example CO
- ▶ Spectrum courtesy of M. Devy
- ▶ $P = 943 \text{ hPa}$; $T = 298 \text{ K}$
- ▶ Spectral data taken from HITRAN 2012
- ▶ Difference in line center about 0.5 %



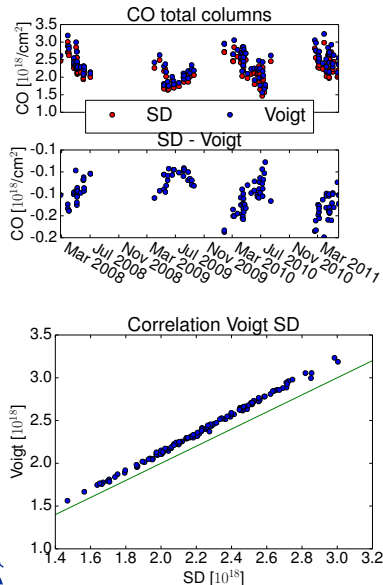
Speed dependence of pressure broadening



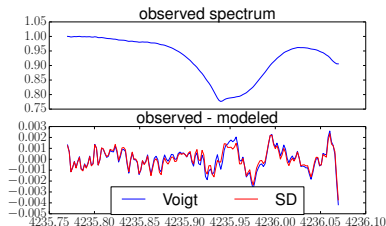
- ▶ Example CO
- ▶ Spectrum courtesy of M. Devy
- ▶ $P = 943$ hPa; $T = 298$ K
- ▶ Spectral data taken from HITRAN 2012
- ▶ Difference in line center about 0.5 %



Effect of speed dependence of pressure broadening on CO



- ▶ Total CO above Bremen
- ▶ Spectrum fitted equally well
- ▶ Difference in total column about 1%
- ▶ Difference can be corrected by scaling



Effect of speed dependence of pressure broadening on CO

Only few molecules in HITRAN have parameters for speed dependency. It seems only CO by the time being.

in sfit4.ctl:

```
fw.lshapemodel = 4
```

```
fw.lshapemodel.sdv = T
```

The spectroscopic input parameters chosen in hbin.input

```
hitran.files = 99
```

```
...
```

```
005_CO/05_hit12.par ...
```

```
aux = ...sdv ...
```

```
aux.sdv.nr = 1
```

```
aux.sdv.files =
```

```
005_CO/05_hit12_SDV.txt ...
```



Effect of speed dependence of pressure broadening on CO

Only few molecules in HITRAN have parameters for speed dependency. It seems only CO by the time being.

in sfit4.ctf:

fw.lshapomodel_4

fw.lsha

The sp

hitran.f

```
READING ATMOSPHERIC LINE LIST FILE...
HITRAN FILE : 04095.941722-04404.058278.hbin
GALATRY FLAG & LINES WITH GALATRY PARAMETERS FOUND : F 0
FCIA FLAG & FCIA LINES FOUND : F 0
SCIA FLAG & SCIA LINES FOUND : F 0
SDV FLAG & LINES WITH SDV PARAMETERS FOUND : T 100
LINEMIXING FLAG & LINES WITH LINEMIXING PARAMETERS FOUND : F 0
COMPUTING CROSS-SECTIONS...
```

...

005_CO/05_hit12.par ...

aux = ...sdv ...

aux.sdv.nr = 1

aux.sdv.files =

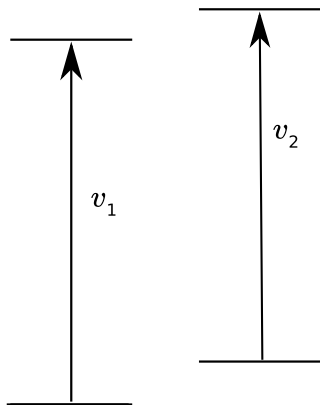
005_CO/05_hit12_SDV.txt ...



Assumption: Lines do not influence each other

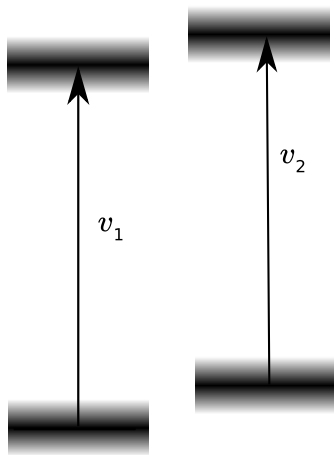


Line mixing



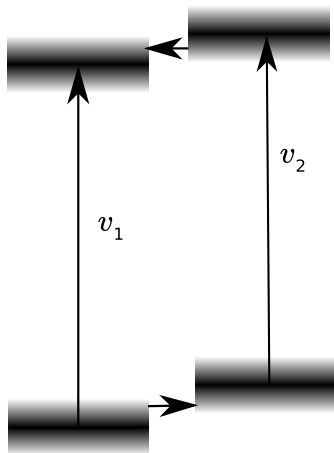
- ▶ Absorption of photon leads to a transition from state 1 to state 2.

Line mixing



- ▶ Absorption of photon leads to a transition from state 1 to state 2.
- ▶ Increase of pressure leads to a broadening of the states, i.e. the same photon may lead to both transitions, ν_1 and ν_2 .
- ▶ The statistical weight of the transitions defines, which transition, ν_1 or ν_2 is more likely.

Line mixing



- ▶ Absorption of photon leads to a transition from state 1 to state 2.
- ▶ Increase of pressure leads to a broadening of the states, i.e. the same photon may lead to both transitions, ν_1 and ν_2 .
- ▶ The statistical weight of the transitions defines, which transition, ν_1 or ν_2 is more likely.
- ▶ Collision couples different states in the same molecule



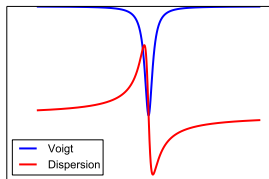
Modeling of line mixing

A band can be calculated (Berman, 1998) using

$$\alpha(\nu) = \frac{N}{\pi} \sum_i p_i \underbrace{\frac{\gamma_i}{(\nu - \nu_i)^2 + \gamma_i^2}}_{\text{Lorentz shape}} + q_i \underbrace{\frac{(\nu - \nu_i)}{(\nu - \nu_i)^2 + \gamma_i^2}}_{\text{Dispersion shape}} \quad (3)$$

The quantities p_i , q_i , γ_i and ν_i define the resulting line shape. Rosenkrantz model (first order expansion):

Parameter	Isolated	Rosenkrantz
p	S	S
q	0	PYS
γ	$P\gamma_0$	$P\gamma_0$
ν_i	$\nu_0 P\delta$	$\nu_0 P\delta$



Modeling of line mixing

In SFIT4 the linemixing is calculated by

$$a(\nu) = \Re(\text{LSMODEL}) + Y_P \Im(\text{LSMODEL})$$

The traditional routine in SFIT4 to calculate the Voigt function does not calculate the imaginary part of the Voigt function. Two ways around:

`fw.lshapemodel = 3` A modified Voigt routine to incorporate line mixing

`fw.lshapemodel = 4` the pCqSDHC model returns real and imaginary part and can therefore be used to calculate the line mixing.



Modeling of line mixing

In `sfit4.ctf`:

```
fw.lshapemodel = 3 or 4
```

```
fw.linemixing = T
```

The spectroscopic parameter Y together with parameters describing the dependency on the pressure P is given in the `hbin` file:

```
hitran.files = 99
```

```
...
```

```
002_CO2/02_hit08_f53.par 005_CO/05_hit12.par ...
```

```
aux = ...lm ...
```

```
...
```

```
aux.lm.nr = 2
```

```
aux.lm.files =
```

```
002_CO2/02_hit08_f53_LM1ST.par
```

```
005_CO/05_hit12_LM1ST.txt
```

```
...
```



Modeling of line mixing

In `sfit4.ctl`:

`fw.lshapemodel = 3` or `4`

`fw.linemixing = T`

The spectroscopic parameter Y together with parameters describing the dependency on the pressure P is given in the

`hbin file`

`hitran file`

...

`002_CO`

`aux =`

...

`aux.lm`

`aux.lm.files =`

`002_CO2/02_hit08_f53_LM1ST.par`

`005_CO/05_hit12_LM1ST.txt`

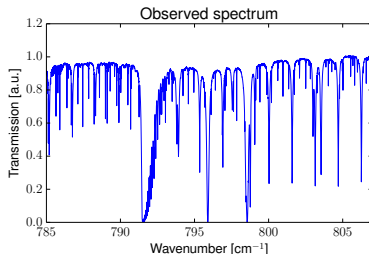
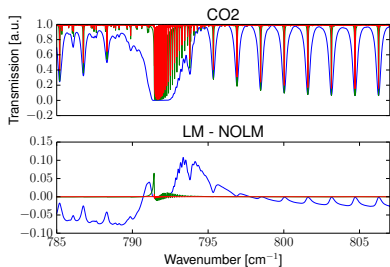
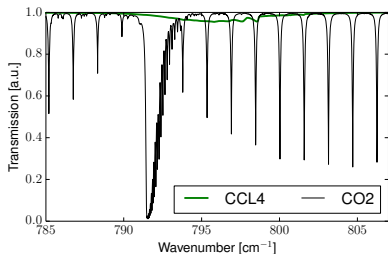
...

```
READING ASCII SPECTRA FILE: spectrum
NFIT BAND SCAN/BAND SCAN_ID SCAN_CODE SPACING NSPAC
RANGE INIT_SNR
1 1 1 1 80257 0.0061000 7 785.000 -
07.000 150.00000
JJB-S12C01AF.DAT 01 DEC 2012 6.1000mK 2.50 mm Ap.ZA=80.257 S/N= 1264 h= 9.1
READING SOLAR LINE LIST FILE...
CALCULATION OF ASTRONOMICAL QUANTITIES ...
BAND, # SOLAR LINES FOUND : 1 236
READING ATMOSPHERIC LINE LIST FILE...
HITRAN FILE : 00780.871900-00811.128100.hbin
GALATRY FLAG & LINES WITH GALATRY PARAMETERS FOUND : F 0
FCIA FLAG & FCIA LINES FOUND : F 0
SCIA FLAG & SCIA LINES FOUND : F 0
SDV FLAG & LINES WITH SDV PARAMETERS FOUND : F 0
LINEMIXING FLAG & LINES WITH LINEMIXING PARAMETERS FOUND : T 378
COMPUTING CROSS-SECTIONS...
```



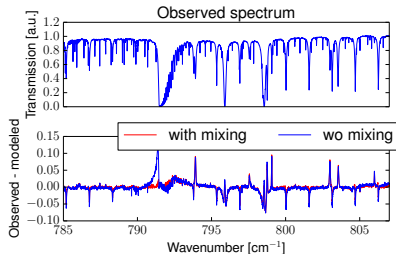
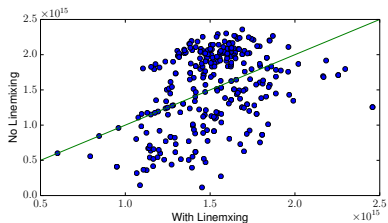
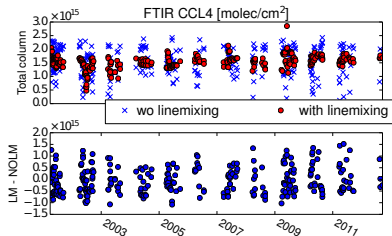
Effect of line mixing in CO₂ on retrieval of CCL₄

- ▶ Artificial spectra of CCL₄ and CO₂
- ▶ Line mixing parameters by Frank Hase (KIT)
- ▶ Line mixing increasing with pressure
- ▶ Mismatch "resembles" CCL₄ band



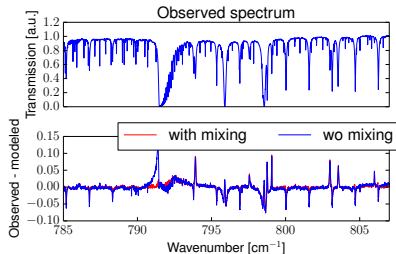
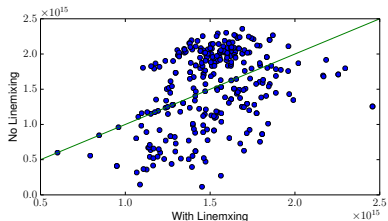
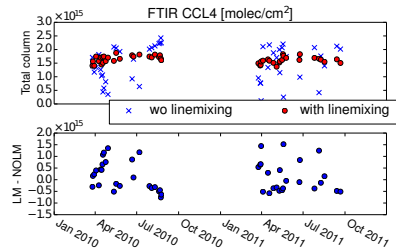
Effect of line mixing in CO₂ on retrieval of CCL₄

- ▶ CCl₄ above Ny Alesund, Spitsbergen
- ▶ Mismatch in CO₂ changes the retrieved value, seasonality and trend in CCL₄.
- ▶ No easy correction possible.



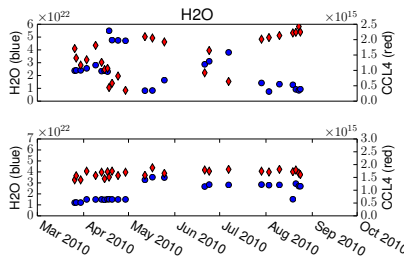
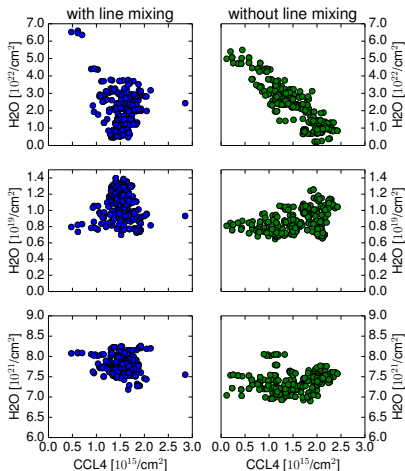
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Effect of line mixing in CO₂ on retrieval of CCL₄

- ▶ Disregarding line mixing effects causes strong anti correlation with H₂O which is not expected, because CCL₄ is a very stable and long-lived gas.



pCqSDHC - **p**artially **C**orrelated **q**uadratic
Speed **D**ependent **H**ard **C**ollision model



pCqSDHC

- ▶ The pCqSDHC function has been proposed by Ngo et.al., 2013 as a replacement for the Voigt line shape model
 - HC - hard collision model
 - qSD - quadratic speed dependency
 - pC - partially correlation of translational and de-phasing effects of collisions
- ▶ The model can be used can be used to calculate line mixing in the Rosenberg approximation

$$S(\nu) = \text{Re}(pCqSDHC) + \gamma \text{Im}(pCqSDHC) \quad (4)$$

-> line-by-line calculation with correction due to line mixing

- ▶ The computational effort is about twice as high as evaluating the Voigt function because speed broadening is modeled as a weighed sum of two Voigt functions
- ▶ contains the Voigt function as a limit



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- ▶ **ONE PROFILE FOR ALL MOLECULES !!!**



Literatur (not complete)

